

Convergence rates of subdivision schemes associated with nonhomogeneous refinement equation

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The purpose of this paper is to investigate multivariate nonhomogeneous refinement equations of the form

$$\varphi(x) = \sum_{\alpha \in \mathbb{Z}^s} a(\alpha) \varphi(Mx - \alpha) + g(x), x \in \mathbb{R}^s,$$

where the vector of functions $\varphi = (\varphi_1, \dots, \varphi_r)^T$ is unknown, g is a given vector of compactly functions on \mathbb{R}^s , a is a finitely supported sequence of $r \times r$ matrices called the refinement mask, and M is an $s \times s$ integer matrix such that $\lim_{n \rightarrow \infty} M^{-n} = 0$. Our purpose is to consider the convergence rates of the subdivision schemes in Sobolev space $(W_p^k(\mathbb{R}^s))^\setminus, (k \leq l \leq \infty)$ and $(L_p(\mathbb{R}^s))^\setminus, (k < l \leq \infty)$ space associated with nonhomogeneous refinement equations mentioned above.