

# Regional climate predictions: Uncertainty and biases

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# Contents

- 1 Introduction
- 2 The paper by Tebaldi et al.
- 3 Our approach
  - The model for the present
  - Future biases
  - Results
- 4 Summary and Outlook

# Starting point

- Predicting the future climate is important for policy making, but difficult because of the complexity of the processes in the ocean, the atmosphere and on the land surface.
- Global models for atmosphere and ocean have a coarse resolution. Regional models allow downscaling by using the output of global models for initial and boundary conditions.
- The number of global and regional models in use is increasing. Each model is run under different emission scenarios. The number of different answers becomes confusing.

# Model selection vs. model combination

- Not all models are equal. A good model should be able to reproduce the current climate and be within the range of other models with its prediction.
- Selecting a single “best” model is not adequate in view of the uncertainty.
- Weighted averaging seems intuitive plausible, but choice of weights is not clear.
- Bayesian methods allow model combinations in a coherent and transparent way.

## Data and distributions

See: Tebaldi et al., J. Climate 18 (2005).

They consider 4 seasons, 22 regions and different scenarios separately. For each season, region and scenario

- Mean of observed temperatures 1961-1990  $\sim \mathcal{N}(\mu, \sigma_0^2)$ .
- Mean of temperatures 1961-1990 from model  $i \sim \mathcal{N}(\mu, \sigma_i^2)$   
( $i = 1, \dots, 9$ ).
- $\mu$  is present mean temperature.
- $\sigma_0^2$  is variance of current climate.
- $\sigma_i^2$  is uncertainty of model  $i$  about present.

$\sigma_0^2$  is assumed to be known. Expect  $\sigma_i^2 > \sigma_0^2$ .

## Data and Distributions, ctd.

- Mean of temperatures for 2071-2100 from model  $i$   
 $\sim \mathcal{N}(\mu + \Delta\mu, (q\sigma_i)^2)$  ( $i = 1, \dots, 9$ ).
- $\Delta\mu$  is climate change.
- $q$  is increase of uncertainty of model  $i$  about future.

All variables are independent given the parameters. A variant introduces correlation between the mean for present and future for the same  $i$ .

Put a noninformative prior on all parameters (except  $\sigma_0$ ) and compute posterior by MCMC. See results on a separate figure.

# Criticism

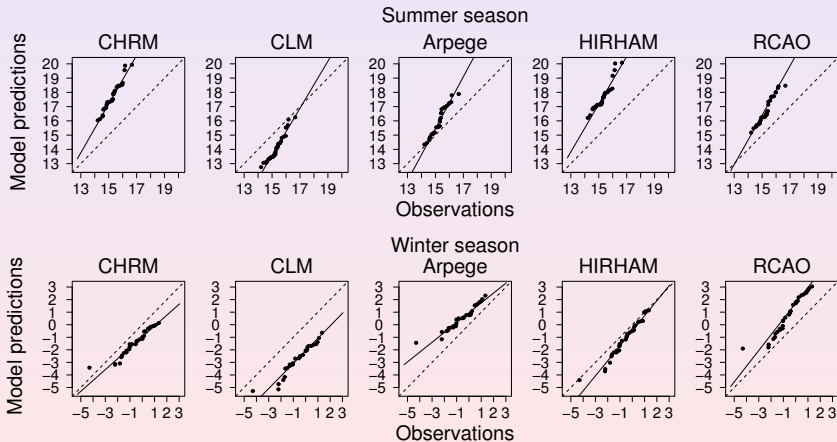
- Interannual variability (for a fixed season and region) is not considered.
- Independence of different models is questionable.
- Biases of the models are not explicitly estimated, but subsumed under the variances  $\sigma_i^2$ .
- Regional models should give better predictions.

## Our approach

- We do not average over 30 years. Need to include possible trends in the model.
- We consider regional models for the alpine region only:  $44^{\circ} - 48^{\circ}\text{N}$ ,  $5^{\circ} - 15^{\circ}\text{E}$ .
- Observations and model output are transformed to the same grid of  $0.5^{\circ}$  ( $\approx 56\text{km}$ ) in both directions.
- Use only 5 models which are based on different global models (or at least different runs of the same model). Otherwise need a hierarchical model because of high correlation between GCM and RCM.



# Biases of control runs



## Model assumptions

- Observed data for  $t = 1961, \dots, 1990$

$$\sim \mathcal{N}(\mu + \gamma(t - t_0), \sigma^2).$$

- Outputs from control run of model  $i$  for the same years

$$\sim \mathcal{N}(\mu + \beta_i + \gamma(t - t_0), b_i^2 \sigma^2).$$

( $\beta_i$  is additive bias,  $b_i$  multiplicative bias)

- All variables are independent: RCM's attempt to reproduce the climate, not the weather of a specific year.
- Unobserved data for  $t = 2071, \dots, 2100$

$$\sim \mathcal{N}(\mu + \Delta\mu + (\gamma + \Delta\gamma)(t - t_0), q^2 \sigma^2).$$

# Assumptions about scenario runs

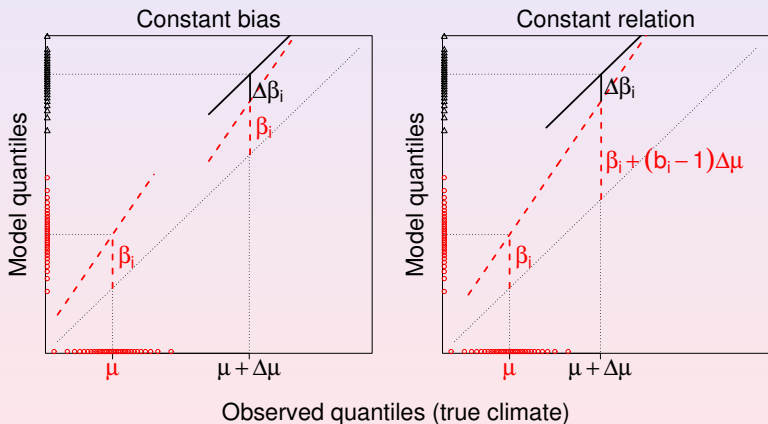
## Two key questions

- How to extrapolate biases to the future?
- Can we allow for changes in the future biases?

## Answers

- At least two extrapolations are possible, that we call constant bias and constant relation.
- Allowing bias changes leads to non-identifiability. Informative priors provide a reasonable solution.

# Graphical illustration



# Mathematical Formulation

## Constant bias:

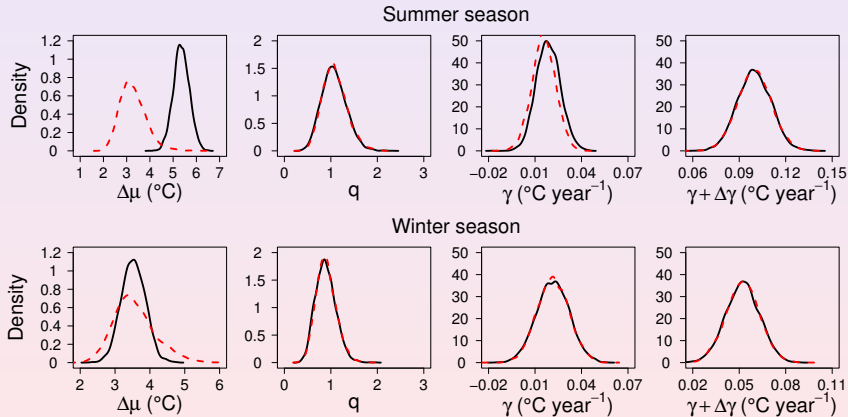
Outputs from run of model  $i$  for years  $t = 2071, \dots, 2100$ :

$$\sim \mathcal{N}(\mu + \Delta\mu + \beta_i + \Delta\beta_i + (\gamma + \Delta\gamma)(t - t_0), (qb_i q_{b_i})^2 \sigma^2).$$

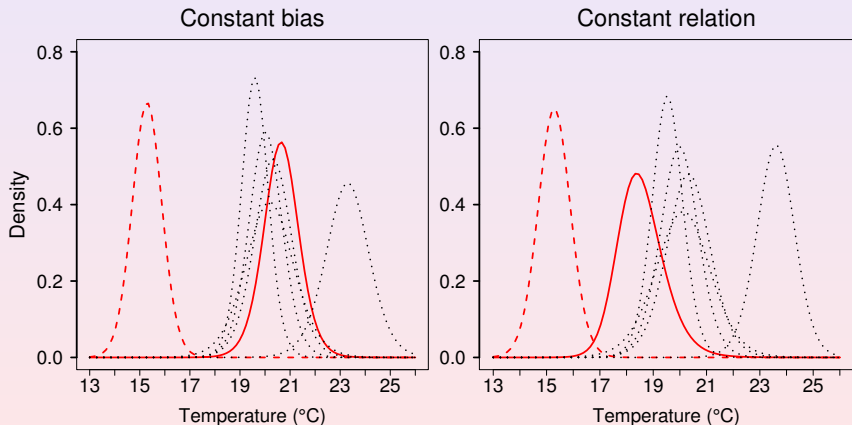
$\Delta\beta_i$  is change in additive bias,  $q_{b_i}$  change in multiplicative bias:  
Put an informative prior on these to keep them near 0 and 1 respectively.

**Constant relation** replaces  $\Delta\mu$  by  $b_i \Delta\mu$ .

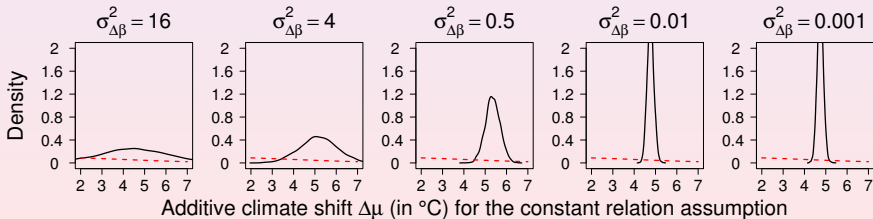
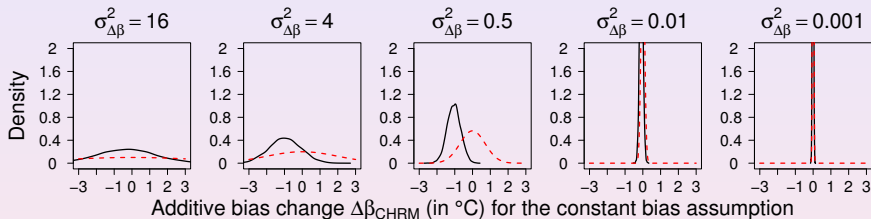
# Posteriors for main parameters



# Posterior predictive densities



# Sensitivity to priors





# Summary

- Statistics for model output from complex data raises new questions.
- Studying distributions instead of mean values gives more information.
- Correcting for biases is important, but assumptions are necessary to do this also for future predictions.
- Is this variance inflation by all models a special feature of the alpine region ?

## Future plans

- More than one scenario. This might help to distinguish between constant bias and constant relation.
- Cross validation for information about reasonable choice of priors for bias changes  $\Delta\beta_i$  and  $q_{b_i}$ .
- Less temporal and spatial averaging.
- Other variables than temperature (multivariate ?)
- Hierarchical modeling for different GCM/RCM combinations (unbalanced designs).