

PROLONGATIONS OF GEOMETRIC OVERDETERMINED SYSTEMS

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ABSTRACT. We show that a wide class of geometrically defined overdetermined semilinear partial differential equations may be explicitly prolonged to obtain closed systems. As a consequence, in the case of linear equations we extract sharp bounds on the dimension of the solution space.



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